# Minimum Volatility Portfolio Construction in Barra Portfolio Manager – A Practical Approach

#### Comparing Minimum Volatility Portfolios with Barra Global Equity Models GEM2 and GEM3

#### Ralph Karels

The concept of minimum volatility portfolios and strategies has become increasingly popular among investors and portfolio managers. In this practical note, we will explain how minimum volatility strategies can be designed in Barra Portfolio Manager using the Barra Global Equity Model 2 (GEM2) as well as the new-generation GEM3, which features the new Volatility Regime Adjustment and Optimization Bias Adjustment techniques.

Start with a pure cash portfolio of USD 100,000,000 and an analysis date of April 28<sup>th</sup> 2012:

Port	tfolio: :h_USD	Variant: Default	Date: Previous Cl	ose (2012/04	Analy 4/28) 🛗 GEM	rsis settings: 3_Cash		
	Tota Portf	il(net)(\$): 100.0 olio Risk: 0,00%	00.000,00 Num	ber of Assets Acti	-Total: 1 ve Risk: 0,00%	Cash (All Curren Predicte	cies %): ed Beta:	100,00% 0,00
	Asset ID	Asset Name	Shares	Price	🖸 Value	🔛 Weight (%)		
			100.000.000,00	1,000	100.000.000,	100,00%		
1	USD	US Dollar	100.000.000,00	1,000	100.000.000,	100,00%		
2								

Next, create a new rebalance profile with a *Single Optimization* rebalancing method, *Max Utility* optimization type and *GEM2* as the risk model. Set the benchmark to cash and the investment universe to the *MSCI World* - *Daily*:

Primary Benchmark	Cash	x	Cash	
Secondary Benchmark	MSCI World - Daily	×	Portfolio	
Market			Cash	
Universe	MSCI World - Daily	×	Portfolio 🔻	

Further constraints can include a minimum number of 100 and a maximum number of 250 stocks to be included in the optimal portfolio:



Trading Constraints > Asset Paring > Min # of Assets					
Min # of Assets	100	Mandatory 🔻			
Max # of Assets	250	Mandatory T			

In order to incorporate an asset level bound of MSCI World weight plus 3%, you need define an asset attribute and upload the respective user data into BPM.

Þ	Setup Asset Attribute				
	Attribute	MinVol_	2	Owner Ralph Karels	
			New	J	
	Association	Miscella	aneous 🔹		
	Value Ture		umber -		
	value Type	Real N	umber	J	
	Max Age	1 mont	h 🔻	)	
Agg	regation Scheme	Market	Value Weighting	)	
	Subscription	Yes		,	
	ou ou i	(D. 11)		)	
	Sharing	Public		J	
	A		В	С	
1	A <attribute name=""></attribute>		B MINVOL_2	С	
1 2	A <attribute name=""> <association></association></attribute>		B MINVOL_2 Miscellaneous	C	
1 2 3	A <attribute name=""> <association> <value type=""></value></association></attribute>		B MINVOL_2 Miscellaneous Real Number	С	
1 2 3 4	A <attribute name=""> <association> <value type=""> <maximum age=""></maximum></value></association></attribute>		B MINVOL_2 Miscellaneous Real Number 1 month	С	
1 2 3 4 5	A <attribute name=""> <association> <value type=""> <maximum age=""> <aggregation sche<="" th=""><th>eme&gt;</th><th>B MINVOL_2 Miscellaneous Real Number 1 month Market Value Weighting</th><th>C</th></aggregation></maximum></value></association></attribute>	eme>	B MINVOL_2 Miscellaneous Real Number 1 month Market Value Weighting	C	
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▲ 1 2 3 4 5 6 7	A <attribute name=""> <association> <value type=""> <maximum age=""> <aggregation sche<br=""><sharing> <asset data=""></asset></sharing></aggregation></maximum></value></association></attribute>	eme>	B MINVOL_2 Miscellaneous Real Number 1 month Market Value Weighting Public <idtype></idtype>	C MINVOL_2	
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1 2 3 4 5 6 7 8 9 10	A <attribute name=""> <association> <value type=""> <maximum age=""> <aggregation sche<br=""><sharing> <asset data=""> <date> FRAAAA1 FRAAAC1</date></asset></sharing></aggregation></maximum></value></association></attribute>	eme>	B MINVOL_2 Miscellaneous Real Number 1 month Market Value Weighting Public <idtype> BARRAID BARRAID</idtype>	C MINVOL_2 3.0786774765965300% 3.5638217040162800%	
1 2 3 4 5 6 7 8 9 10 11	A <attribute name=""> <association> <value type=""> <maximum age=""> <aggregation sche<br=""><sharing> <asset data=""> <date> FRAAAA1 FRAAAC1 FRAAAH1</date></asset></sharing></aggregation></maximum></value></association></attribute>	eme>	B MINVOL_2 Miscellaneous Real Number 1 month Market Value Weighting Public <idtype> BARRAID BARRAID BARRAID</idtype>	C MINVOL_2 20120428 3.0786774765965300% 3.5638217040162800% 3.0482141091156100%	
1 2 3 4 5 6 7 8 9 10 11 12	A <attribute name=""> <association> <value type=""> <maximum age=""> <aggregation sche<br=""><sharing> <asset data=""> <date> FRAAAA1 FRAAAA1 FRAAAA1 FRAAAH1 GERAPC1</date></asset></sharing></aggregation></maximum></value></association></attribute>	eme>	B MINVOL_2 Miscellaneous Real Number 1 month Market Value Weighting Public <idtype> BARRAID BARRAID BARRAID BARRAID</idtype>	C MINVOL_2 20120428 3.0786774765965300% 3.5638217040162800% 3.0482141091156100% 3.2218393630035600%	
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1 2 3 4 5 6 7 8 9 10 11 12 13 14	A <attribute name=""> <association> <value type=""> <maximum age=""> <aggregation sche<br=""><sharing> <asset data=""> <date> FRAAAA1 FRAAAA1 FRAAAC1 FRAAAH1 GERAPC1 GERAPA1 UKIFEU1</date></asset></sharing></aggregation></maximum></value></association></attribute>	eme>	B MINVOL_2 Miscellaneous Real Number 1 month Market Value Weighting Public <idtype> BARRAID BARRAID BARRAID BARRAID BARRAID BARRAID BARRAID</idtype>	C MINVOL_2 20120428 3.0786774765965300% 3.5638217040162800% 3.0482141091156100% 3.2218393630035600% 3.4809897048684700% 3.6202948086236700%	

You can add a factor-level constraint on industries of minimum 0 and maximum 10% weight. Finally, tick the *Invest All Cash* Box in the *Cash Rules* section:



Cash Rules > Cash Settings > Invest All Cash	
Cash In/Out	🗹 Invest All Cash

Note that by not defining any expected returns (alphas), the optimizer will effectively minimize risk (given the specified constraints), making the optimized portfolio a minimum volatility one. To run the optimization, save the rebalance profile defined above and start the *Rebalance Tool*:

	Rebalance Too
Date: Profile:	
Previous Close (2012/04/28) MinVol_GEM2	
thod: Single Optimization Type: Max Utility Risk Model: GEM	2L
	Date: Profile: Previous Close (2012/04/28) MinVol_GEM2 thod: Single Optimization Type: Max Utility Risk Model: GEM

The optimal portfolio contains 100 assets and an ex-ante annualized total risk of 10.32%. For the same date, the MSCI World has an ex-ante annualized total risk of 18.49% under GEM2 - a risk reduction of 8.17 percent points.

	Status	Iteration	Primary Benchmark	Number Of Assets	Active Risk	Turnover
1	Success	Iteration 2	Cash	100	10,32%	100,00%

The largest holding in the optimized portfolio is Kimberley Clark Corp (1.92%), and the smallest is Motorola Mobility (0.30%). Industry exposures are concentrated in Banks, Telecomms, Pharma, Utilities and Food & Beverages:

Por	tfolio: Variant:	Date:	Analysis settings:
Mir	Vol_Opt_GEM2	Previous Close (2012/04/28)	GEM2L_BM_Cash
Fac	tor Type Industry		
	Factor	Portfolio Net Exposure	Portfolio Long Exposure
1	Industry	1,00	1,00
2	- Banks	0,10	0,10
3	<ul> <li>Telecommunication Services</li> </ul>	0,10	0,10
4	Pharmaceuticals and Life Sciences	0,10	0,10
5	- Utilities	0,10	0,10
6	<ul> <li>Food Beverage and Tobacco</li> </ul>	0,10	0,10
7	Household and Personal Products	0,09	0,09
8	<ul> <li>Food and Staples Retailing</li> </ul>	0,08	0,08
9	Retailing	0,07	0,07
10	<ul> <li>IT Services and Software</li> </ul>	0,06	0,06

A risk decomposition using the Correlation Risk Attribution methodology shows that the majority of the optimized portfolio's total risk of 10.32% stems from common factor risk (9.32%), with minor contributions from specific risk (0.23%) and currency (0.77%):

	Risk Source	[Net] Active Risk	[Net] Active Correlation	[Net] Active Risk Contribution
1	🔲 Total	10,32%	1,00	10,32%
2	Local Excess	10,21%	0,94	9,55%
3	<ul> <li>Market Timing</li> </ul>	0,00%	0,00	0,00%
4	🕞 Residual	10,21%	0,94	9,55%
5	Common Factor	10,09%	0,92	9,32%
6	Industry	2,17%	-0,31	-0,67%
7	Risk Indices	9,28%	-0,57	-5,28%
8	Country	3,68%	0,10	0,35%
9	- World	18,65%	0,80	14,92%
10	- Factor Interaction	N/A	N/A	N/A
11	Specific	1,54%	0,15	0,23%
12	Currency	3,69%	0,21	0,77%
13	Currency/Market Interaction	N/A	N/A	N/A

To replicate the analysis using GEM3 as the risk model, create a new rebalance profile with the same constrains as the ones defined above, but using the GEM3 model:

Image: Second system       Date:       Profile:         Portfolio:       Date:       Profile:         Cash_USD       Previous Close (2012/04/28)       Image: MinVol_GEM3         Rebalance Method:       Single Optimization       Type:       Max Utility       Risk Model:       GEM3L/GEM21	2		Rebalance Tool
Portfolio:     Date:     Profile:       Cash_USD     Previous Close (2012/04/28)     MinVol_GEM3       Rebalance Method:     Single Optimization     Type:     Max Utility     Risk Model:     GEM3L/GEM21	$\bigcirc$	985	
Cash_USD Previous Close (2012/04/28) MinVol_GEM3 Rebalance Method: Single Optimization Type: Max Utility Risk Model: GEM3L/GEM2I	Portfolio:	Date:	Profile:
Rebalance Method: Single Optimization Type: Max Utility Risk Model: GEM3L/GEM2I	Cash_USD	Previous Close (2012/04/28)	MinVol_GEM3
	Cash_USD Rebalance Met	Previous Close (2012/04/28)	MinVol_GEM3 Jtility Risk Model: GEM3L/GE

The GEM3 optimal portfolio contains 100 assets and an ex-ante annualized total risk of 8.37%. For the same date, the MSCI World has an ex-ante annualized total risk of 16.55% under GEM3. A risk reduction of 8.18 percent points was achieved - very similar to the GEM2 Case (8.17 percent points of risk reduction) but with lower total risk levels:

	Status	Iteration	Primary Benchmark	Number Of Assets	Active Risk	Turnover
1	Success	Iteration 1	Cash	100	8,37%	100,00%

The largest holding in the optimal portfolio is Kimberly Clark Corp (2.66%), and the smallest is Coca Cola (0.02%). Industry exposures are similar to the ones obtained when optimizing with GEM2 – with the notable exception of Banks:



			Factor Expos	sure
	Port	folio: Variant: D Vol_Opt_GEM3	ate: Previous Close (2012/04/28)	Analysis settings: GEM2L_BM_Cash
	Fact	or Type Industry	Name: Previous Close Date: 2012/04/28	e
l		Factor	Portiono wet exposure P	ortfolio Long Exposure
l	1	Industry	1,00	1,00
l	2	<ul> <li>Food and Staples Retailing</li> </ul>	0,10	0,10
l	3	- Utilities	0,10	0,10
l	4	Telecommunication Services	0,10	0,10
l	5	Pharmaceuticals and Life Sciences	0,10	0,10
l	6	Household and Personal Products	0,10	0,10
l	7	Food Beverage and Tobacco	0,10	0,10
l	8	Retailing	0,08	0,08
	9	Transportation Non-Airline	0,07	0,07
	10	Hotels Restaurants and Leisure	0,05	0,05

A risk decomposition using the Correlation Risk Attribution methodology shows a similar picture compared with GEM2: The majority of the portfolio's total risk of 8.37% stems from common factor risk (7.65%) and minor contributions from specific risk (0.28%) and currency (0.43%):

		Risk Attribution						
Portfolio: Variant: MinVol_Opt_GEM3		Date: Anal Previous Close (2012/04/28)		ysis settings: 13_Cash				
Portfolio Scope Net 🔻								
	Risk Source	[Net] Active Risk	[Net] Active Correlation	[Net] Active Risk Contribution				
1	🗖 Total	8,37%	1,00	8,37%				
2	Local Excess	8,38%	0,95	7,94%				
3	<ul> <li>Market Timing</li> </ul>	0,00%	0,00	0,00%				
4	🔲 Residual	8,38%	0,95	7,94%				
5	Common Factor	8,24%	0,93	7,65%				
6	🖸 Industry	1,79%	-0,22	-0,39%				
7	🔛 Risk Indices	7,74%	-0,56	-4,37%				
8	Country	3,25%	0,29	0,93%				
9	🖸 World	14,73%	0,78	11,48%				
10	- Factor Interaction	N/A	N/A	N/A				
11	Specific	1,53%	0,18	0,28%				
12	Currency	2,73%	0,16	0,43%				
13	Currency/Market Interaction	N/A	N/A	N/A				

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